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Pinto, R. F., Catalanotti, G., & Camanho, P. P. (2016). Measuring the intralaminar crack resistance curve of fibre reinforced composites at extreme temperatures. *Composites Part A: Applied Science and Manufacturing*, 91(1), 145-155. <https://doi.org/10.1016/j.compositesa.2016.10.004>

### Published in:

Composites Part A: Applied Science and Manufacturing

### Document Version:

Early version, also known as pre-print

### Queen's University Belfast - Research Portal:

[Link to publication record in Queen's University Belfast Research Portal](#)

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# Measuring the intralaminar crack resistance curve of fibre reinforced composites at extreme temperatures

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## Abstract

This work focuses on the development of methods to measure the intralaminar fracture toughness of IM7/8552 CFRP at extreme temperatures. The size effect law of scaled double-edge-notched (DEN) specimens is used to obtain the crack resistance curves associated with longitudinal failure of polymer composites. The compressive and tensile crack resistance curves are determined and compared to those measured at room temperature. Scanning electron microscopy is used to analyse the fracture surface of tensile DEN specimens as a means to understand the damage mechanisms involved and their dependence on temperature variations. It is shown that the methods proposed enable the measurement of the crack resistance curve under different environment conditions. The results obtained can be used in analytical models to evaluate the integrity of composite structures at extreme temperatures.

*Keywords: Fibre reinforced materials, Fracture mechanics, R-curve, Intralaminar fracture toughness, Size effect, Temperature, Material characterization, Elastic properties, Scanning electron microscopy*

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## 1. Introduction

Recent analysis models that predict fracture of composite structures require the values of the fracture toughness associated with different failure modes [1, 2, 3, 4]. In particular, the intralaminar fracture toughness is required not only for material screening and characterization but also for identifying the softening constitutive relation that simulates longitudinal tensile and compressive failure [1, 5].

While recent work has been performed on the measurement of crack resistance curves (R-curves) associated with longitudinal fracture at room temperatures [6, 7], there is no information on the effects of extreme temperatures on the corresponding R-curves. Taking into account that the structural integrity must be preserved under different working scenarios and environments, in particular at extreme temperatures, the objective of this paper is to study how extreme temperatures affect the crack resistance curve of polymer composites that fail under longitudinal tension and compression. Taking the commercial aerospace industry as an example, composite materials need to fulfil their structural requirements at room temperature, at flight cruise altitude where temperatures can be lower than  $-50^{\circ}\text{C}$ , while also reaching high temperatures at the vicinity of the engine and engine fluid flow systems.

Temperature does not affect the carbon fibre properties but has influence on the polymer matrix and on the fibre-matrix interface [8], thus changing the mechanical response of the composite system. Due to the complex behaviour of composite materials under different thermal conditions, the mechanical response under temperature variations is difficult to predict.

The dependence of composite materials modulus and stiffness on temperature is well known and documented [9, 10, 11]. As temperature increases, the polymer Young's modulus suffers a transition from 'glass-like' to 'rubber-like' and the abrupt drop in modulus takes place at the glass transition temperature, denoted as  $T_g$ . The strength of composite materials is directly connected to the intrinsic properties of its constituents, even if fibres are almost tempera-

ture insensitive the overall mechanical properties of the composite are affected due to the matrix/fibre interface property changes. In fact, as the temperature increases, the matrix stiffness decreases, which causes a decrease of the laminate's strength [12, 13, 14]. A study conducted by Whitley and Gates [15] has  
35 shown that for cryogenic temperatures the shear modulus and strength increase as temperature decreases.

Kim et al. [16, 17] investigated the effects of temperature on the mode I and mode II interlaminar fracture of CFRP. As temperature increases,  $\mathcal{G}_{IC}$  decreases slightly for the unidirectional laminate  $[0]_{24}$  but increases for the other  
40 two laminates with different ply orientations [16]. However, as temperature increases,  $\mathcal{G}_{IIC}$  decreases for all three laminates considered.

Despite the aforementioned work, no relevant work has been performed to measure the R-curve at extreme temperatures. Commonly used procedures to measure the tensile fracture toughness and tensile crack resistance curve (R-curve) use approaches developed for metals such as the compact tension (CT)  
45 curve) and the compact compression (CC) test specimens [6, 7]. The use of these specimens together with proper reduction methods on brittle materials provides accurate results [7, 18]. However, with the introduction of new tougher resins, higher loads are required for crack propagation, which may lead to buckling at  
50 the un-notched end of the test specimen [18].

Recent work provides reliable test methods to accurately obtain the R-curve associated with the tensile and compressive longitudinal failure [19, 20]. In the last case, failure corresponds to the formation and propagation of kink bands, which brings new challenges to the measurement of the compressive fracture  
55 toughness and crack resistance curve [21, 22].

The present work relies on the size-effect method initially proposed by Bažant [23] based on the relation of the size effect law with the R-curve. This method was extended by Catalanotti et al. [19, 20, 24] to measure the intralaminar R-curves in fibre reinforced composites and is used to experimentally determine  
60 the R-curve of IM7/8552 CFRP at extreme temperatures. The results are then compared with the tensile and compressive R-curve of the same material mea-

measured at room temperature following the same method [19, 20]. Since these new methods do not require any form of tracking of the crack size during testing, they can be used in working conditions under several extreme environment scenarios, where some type of enclosure for the specimens is involved. Applying these new approaches it is possible to achieve accurate measurements with near zero visibility to the specimen undergoing the test.

## 2. Materials and methods

### 2.1. Analytical model

For a two-dimensional orthotropic body with  $x$  and  $y$  as the preferred axes of the material, the energy release rate (ERR) in mode  $I$  necessary for crack propagation in the  $x$ -direction can be described using the following equation [25]:

$$\mathcal{G}_I = \frac{1}{E} \mathcal{K}_I^2 \quad (1)$$

where  $\mathcal{K}_I$  is the stress intensity factor and  $\acute{E}$  is the equivalent modulus defined as:

$$\acute{E} = \left( s_{11}s_{22} \frac{1+\rho}{2} \right)^{-1/2} \lambda^{1/4} \quad (2)$$

where  $s_{lm}$  are the components of the compliance matrix in the  $x - y$  coordinate system,  $\lambda$  and  $\rho$  are two dimensionless elastic parameters that take into account the anisotropy of the material and are defined as [25]:

$$\lambda = \frac{s_{11}}{s_{22}}, \quad \rho = \frac{2s_{12} + s_{66}}{2\sqrt{s_{11}s_{22}}} \quad (3)$$

Note that the compliances are functions of the temperature and therefore  $\lambda$  and  $\rho$  vary with the applied temperature.

The stress intensity factor,  $\mathcal{K}_I$  in Eq. (1) is a function of  $\rho$ , of the remote stress  $\sigma$  and of the geometry of the specimen [25, 26] and it reads:

$$\mathcal{K}_I = \sigma \sqrt{wk}(\alpha, \rho, \lambda) \quad (4)$$

where  $\alpha = a/w$  is the shape-parameters and  $k$  is the correction factor that depends on the geometry and orthotropy of the material. Replacing (4) in  
85 equation (1),  $\mathcal{G}_I$  yields:

$$\mathcal{G}_I = \frac{1}{E} w \sigma^2 k^2 = \frac{1}{4wE} \left( \frac{Pk}{t} \right)^2 \quad (5)$$

where  $t$  is the thickness of the specimen and  $P$  is the applied load. Assuming that  $k$  is an increasing function of the crack length (the specimen has a positive geometry), the size effect can be used to measure the fracture toughness of the material [27] using (5):

$$\mathcal{G}_I(\Delta a) = \frac{P^2}{4wt^2E} k^2 \left( \alpha_0 + \frac{\Delta a}{w}, \rho, \lambda \right) \quad (6)$$

90 where  $\alpha_0 = a_0/w$ .

For different geometries  $w_n$ , the crack driving-force curves  $\mathcal{G}_I$  corresponding to the peak loads  $P_{un}$  are tangent to the R-curve. This is the basis of the method used to measure the R-curve  $\mathcal{R}$ . The peak load  $P_u$  and thus the ultimate remote stress  $\sigma_u = P_u/(2wt)$  can be obtained using Eq. (7):

$$\begin{cases} \mathcal{G}_I(\Delta a) = \mathcal{R}(\Delta a) \\ \frac{\partial \mathcal{G}_I(\Delta a)}{\partial \Delta a} = \frac{\partial \mathcal{R}(\Delta a)}{\partial \Delta a} \end{cases} \quad (7)$$

95 Assuming that the size effect law is known  $\sigma_u = \sigma_u(w)$  and replacing Eq. (5) in the first of Eq. (7) results in:

$$\mathcal{R}(\Delta a) = \frac{1}{E} w \sigma_u^2 k^2 \quad (8)$$

Eq. (8) is valid for all values of  $w$ . Differentiating Eq. (8) [27] with respect to  $w$ , assuming that geometrically similar specimens are tested ( $\alpha_0$  is independent of the width,  $w$ ) and knowing that the R-curve does not depend on  $w$  ( $\frac{\partial \mathcal{R}}{\partial w} = 0$ ),

100 results in:

$$\frac{\partial}{\partial w} (w \sigma_u^2 k^2) = 0 \quad (9)$$

this equation can be solved for  $w = w(\Delta a)$  which when replaced in (8) yields the R-curve,  $\mathcal{R}(\Delta a)$ .

According to Bažant and Planas [27], the size effect law should be determined testing geometrically identical samples and applying one of the three types of fitting approaches: (i) the bilogarithmic regression, (ii) the linear regression I or (iii) the linear regression II. Table 1 shows the formulas for the calculation of the length of the fracture zone  $l_{f_{pz}}$  and for the fracture toughness  $\mathcal{R}_{SS}$  for each regression fit normally used where  $k_0 = k|_{\alpha=\alpha_0}$  and  $\dot{k}_0 = \partial k / \partial \alpha|_{\alpha=\alpha_0}$ .

[Table 1 about here.]

Figure 1 shows the geometry of a double edge notched (DEN) compression and tension specimen. The width of the specimens is  $2w$  and the initial crack length is  $a_0$ . The length of the compression specimen is  $3w$  and the length of the tension specimen is  $2l$ .

[Figure 1 about here.]

A calculation of the correction factor is presented in [19] and [20] for both the compressive and tensile specimen.

## 2.2. Experimental testing

All tests were performed in an Instron 4208 testing machine equipped with a 100 kN load cell and fitted with a Instron environmental chamber model 3119-007. For the high temperature tests, the two electrical resistances within the chamber were used to achieve the required temperature of 100 °C. For the low temperature, liquid nitrogen ( $N_2$ ) was injected inside the chamber until the pre-set temperature value of -50 °C was achieved. This process is controlled by an automatic solenoid valve that continuously manages the inflow of the cooling fluid.

To secure the tensile specimens, an extension was manufactured and mounted between the load cell and the upper grip. Such extension allows enough clearance for the vertical movement and also makes possible to use 250 mm long

specimens whilst having the specimen subjected to the [desired](#) temperature.

130 For the compressive specimens, a lower extension adapter was designed and manufactured to increase the height of the bottom section of the compression rig component. This [adapter](#) is composed of a self alignment mechanism that sits on top of the extension, which in turn bolts directly into the Instron 4208 base table. The self-alignment mechanism consists of two parts connected by a

135 spherical joint, the top part is equipped with a tungsten-carbide insert in order to prevent indentation when in contact with the specimen. [The](#) bottom part of this assembly is fixed to the bottom extension, which is then bolted to the Instron 4208 testing machine (Figure 2).

[Figure 2 about here.]

140 For all tests, the specimens were placed inside the chamber and the chamber temperature control was set to the desired temperature. After the chamber thermocouple reading output reached the [desired](#) temperature value, the specimen was allowed to stabilize for a period [of no less than](#) 30 minutes prior to testing. Compensation for material [shrinkage](#) (-50 °C) and/or swelling (100 °C) during

145 stabilization was performed manually using the Instron 4208 control panel.

### 2.3. Material

Hexcel’s IM7/8552 carbon epoxy unidirectional tape with a nominal ply thickness of 0.125 mm was used. The material was cured in a hot plate press according to the manufacturer’s specifications, which consists in submitting the

150 material to three temperature stages: (i) 110 °C for one hour followed by (ii) 180 °C for two hours and finally (iii) cool down at 3 °C/min until room temperature. During the curing cycle, a pressure of 7 bar is applied to the material.

The IM7/8552 elastic material properties at room temperature were obtained in previous investigations [28]. [Tests were also](#) conducted to measure the elastic

155 [properties at low and high temperatures following the applicable standards \[29, 30\].](#) [These moduli are](#) required to determine the R-curve [at each](#) temperature. The tests to measure  $E_1$  at extreme temperatures faced difficulties resulting from

debonding of the strain gauges and fracture of its connectors. This property was taken as constant since  $E_1$  is mainly controlled by the stiffness of the fibres, which is unlikely to change substantially with temperature. Table 2 reports the elastic properties where  $E_1$  and  $E_2$  are respectively the longitudinal and transverse modulus,  $G_{12}$  is the shear modulus, and  $\nu_{12}$  is the major Poisson's ratio.

[Table 2 about here.]

#### 2.4. Compressive R-curve

Samples of Hexcel IM7/8552 carbon fibre composite material were cut using a diamond coated mechanical saw from a plate with a  $[0/90]_{8s}$  layup and a nominal thickness of 4 mm. Notches in the samples were then machined using a vertical mill equipped with a 1 mm diameter drill bit. The crack faces separation was 1 mm. This value provides enough clearance so that the adjacent crack faces do not come in contact during compressive testing, thus invalidating the test. Also, the shape of the crack tip is unlikely to affect the value of the fracture toughness in compression where the specimens fail by kink-band formation [31].

Six different configurations were used, corresponding to references  $A$  to  $F$  (Figure 3). A total of 36 specimens were tested, 18 specimens at  $-50^\circ\text{C}$  and another 18 specimens at  $100^\circ\text{C}$  with three samples per each configuration.

[Figure 3 about here.]

Compressive tests were carried inside the Instron 3119-007 environmental chamber under displacement control and at a speed of 0.5 mm/min. In order to use the analytical model developed by Catalanotti et al. [19], which assumes a frictionless contact between the specimen and the tool(s), a very thin layer of molybdenum disulphide ( $\text{MoS}_2$ ) was applied at the specimen extremities to decrease friction (Figure 4).

[Figure 4 about here.]

185 *2.5. Tensile R-curve*

IM7/8552 material plates with  $[90/0]_{8s}$  layup and nominal thickness of 4 mm were cut with a diamond-coated mechanical saw. The tensile samples were then machined in order to obtain a double notch using a vertical mill with a 1 mm drill bit. No sharp cut was performed in the crack radius of the specimens after  
 190 machining the crack. It has been shown that the fracture toughness measured using a sharp crack or a 1 mm radius notch is virtually the same [32] and, at peak load, the crack may be considered sharp [33].

For the tensile tests, a total of five geometries were used labeled from *A* to *E* (Figure 5), three samples from each geometry and for each temperature were  
 195 tested resulting in a total of 30 specimens, of which 15 were tested at -50 °C and another 15 were tested at 100 °C.

[Figure 5 about here.]

The Instron environment chamber was used to perform all tests at the required temperatures under displacement control at a speed of 1 mm/min. Two  
 200 small pieces of a high-grit sandpaper were used at both ends of the specimens to increase the friction between the specimen and the top and bottom grips (Figure 6).

[Figure 6 about here.]

*2.6. Scanning electron microscopy*

205 The fracture surfaces of the DEN tensile specimens were examined using a FEI Quanta 400 series environment scanning electron microscope to investigate any distinct features resulting from submitting these samples to different testing temperatures. Observations were performed on the fracture surfaces of the tested samples at -50 °C and 100 °C.



### 210 3. Experiments

#### 3.1. Experimental results for DEN compressive tests

Figure 7(a) shows one specimen from each geometry after testing at -50 °C, and Figure 7(b) shows the specimens tested at 100 °C.

[Figure 7 about here.]

215 Representative load vs displacement curves can be seen in Figure 8 for the specimens tested at -50 °C, and in Figure 9 for the samples tested at 100 °C. There is one curve for each of the six tested geometries at -50 °C and 100 °C. Table 3 shows the summary of the results for the two temperatures under investigation. The notation used is  $C$ - $X$ - $0Y$ - $Z$ , where  $C$  represents the type of test  
220 (compression),  $X$  is the specimen configuration, which ranges from  $A$  to  $F$ ,  $Y$  is the specimen number, and  $Z$  takes the letter  $C$  for -50 °C ‘cold’ temperature or  $H$  for 100 °C ‘hot’ temperature.

[Figure 8 about here.]

[Figure 9 about here.]

225 [Table 3 about here.]

#### 3.2. Experimental results for DEN tensile tests

Figures showing the fracture surface of the specimens tested in tension can be observed in Figure 10(a). This figure shows one specimen of each tested configuration at -50 °C. Figure 10(b) shows the fractured specimens tested at 100 °C.  
230 No significant differences on the macroscopic failure surface are observed.

[Figure 10 about here.]

Figure 11 and Figure 12 depict two examples of the load vs. displacement curves. There are five curves on each graph corresponding to one of each tested configuration at -50 °C and 100 °C. Table 4 reports the results obtained experimentally for each temperature. The notation used is  $T$ - $X$ - $0Y$ - $Z$ , where  $T$   
235

represents the type of test (tension),  $X$  is the specimen geometry which ranges from  $A$  to  $E$ ,  $Y$  is the specimen number and  $Z$  represents the temperature under investigation, which is identified as  $C$  for -50 °C ‘cold’ temperature or  $H$  for 100 °C ‘hot’ temperature.

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[Figure 11 about here.]

[Figure 12 about here.]

[Table 4 about here.]

#### 4. Data analysis and discussion

##### 4.1. Obtaining the compressive $R$ -curve from size effect

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Obtaining the  $R$ -curve of the material using the size effect method requires the knowledge of the size effect law, which dictates the relation between the nominal remote stress and the geometry of the sample i.e.  $\sigma_u = \sigma_u(w)$ .

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The different types of regression plots described by Bažant and Planas [27] were investigated using the data obtained experimentally. Figures 13(a) and 13(b) show the experimental data and the best fitting curves for the regression methods investigated at -50 °C and 100 °C, respectively. It can be observed that the size effect law that best fits the data is the bilogarithmic for both temperatures under study with a coefficient of determination of  $R^2 = 0.446$  and  $R^2 = 0.4597$ . The Levenberg-Marquardt algorithm implemented in Matlab [34] is used to assess the goodness of the fit. The Interval Confidence (IC) of the fitting function at 90% is calculated and reported in Figures 13(a) and 13(b). This will later allow the calculation of the Interval of Confidence for the  $R$ -curves. After the determination of the size effect law, Eq. (9) can be solved for  $w = w(a)$ , all the required parameters of the equation are known and can be seen in Table 5.

260

[Figure 13 about here.]

[Table 5 about here.]

Using Eq. (8) with the known values and with  $w = w(a)$ , the R-curve of the laminate,  $\mathcal{R}$  is calculated. Multiplying by 2 the value of  $\mathcal{R}$  for every  $\Delta a$ , the fracture toughness of the  $0^\circ$  ply ( $\mathcal{R}_0$ ) is obtained. Figures 14 and 15 show the result of applying this methodology to obtain the R-curve at the temperatures under study.  $\mathcal{R}_0$  is the envelope of the crack driving forces.

[Figure 14 about here.]

[Figure 15 about here.]

The steady-state value for the fracture toughness is obtained using the following:

$$\mathcal{R}_{SS}^0 = \lim_{w \rightarrow \infty} \mathcal{R}_0 \quad (10)$$

The steady state fracture toughness value ( $\mathcal{R}_{SS}$ ) reads 60.85 kJ/m<sup>2</sup> at -50 °C and 43.47 kJ/m<sup>2</sup> at 100 °C. The length of the fracture process zone,  $l_{fpz}$  is obtained following Bažant and Planas [27]:

$$l_{fpz} = \frac{k_0}{2k'_0} w_0 \quad (11)$$

where  $k_0$  is  $k(\alpha_0)$ ,  $k'_0$  is  $k'(\alpha_0)$  and  $w_0$  is the constant of Bažant size effect law, which for the bilogarithmic regression takes the value of  $N$ . The length of the fracture toughness zone,  $l_{fpz}$  is then calculated to be equal to 0.84 mm at -50 °C and 1.78 mm at 100 °C.

The compressive R-curve for IM7/8552 at the temperatures studied are shown alongside the results obtained by Catalanotti et al. [19] for the same material system (Figure 16).

[Figure 16 about here.]

#### 4.2. Obtaining the tensile R-curve from size effect

Similar to what happened with the compressive R-curve, the relation between the nominal remote stress and the geometric parameters of the specimens used must be known ( $\sigma_u = \sigma_u(w)$ ) to calculate the tensile R-curve.

Bazant and Planas [27] describe three approaches that were investigated to find the best fit for the tensile results at the two temperatures. Figure 17(a) and Figure 17(b) show the experimental data and the best fitting curve for the investigated methods at -50 °C and 100 °C. The law that best fits the data is the bilogarithmic for both temperatures under study with a coefficient of determination of  $R^2 = 0.8404$  and  $R^2 = 0.8191$ , where the parameters of fitting are shown in Table 6.

[Figure 17 about here.]

[Table 6 about here.]

After determining the best size effect law for the measured data, the procedure previously described was used to obtain the tensile R-curve of the 0° ply. This is shown in Figures 18 and 19 where  $\mathcal{R}_0$  is the envelope of the tensile crack driving forces.

[Figure 18 about here.]

[Figure 19 about here.]

The steady state fracture toughness value ( $\mathcal{R}_{SS}$ ) reads 62.50 kJ/m<sup>2</sup> at -50 °C and 166.40 kJ/m<sup>2</sup> at 100 °C. The length of the fracture process zone,  $l_{fpz}$  is obtained following Bazant and Planas [27], as previously done for the compressive R-curve, which is equal to zero at -50 °C and 0.72 mm at 100 °C.

The tensile R-curve for the IM7/8552 0° ply at the extreme temperatures are shown in Figure 20. This figure includes the data obtained by Catalanotti et al. [20] at room temperature.

[Figure 20 about here.]

#### 4.3. Discussion

The results reported in Table 2 show that the transverse modulus decreases with temperature, as indicated by a decrease from 10.61 GPa at -50 °C to

7.96 GPa at 100 °C. The same trend is observed for the shear moduli. Changing the temperature directly affects the adhesion between fibre and matrix. The key reason may lie in the different coefficient of thermal expansion of each material. The longitudinal Poisson's ratio remains almost constant throughout the temperatures considered in the study.

The tests conducted to measure the compressive fracture toughness show the scatter that is typical in compressive tests of polymer composite materials. The procedure described in Koerber et al. [35] was used to minimize not only the scatter but also the probability of premature failure of the specimen. Furthermore, previous investigations where back-to-back strain gages were used [19] indicted that the compressive test set-up was not inducing bending in the specimen. The results shown in Figure 16 indicate that, decreasing the temperature from 25 °C to -50 °C, the compressive fracture toughness does not change. However, increasing the temperature from 25 °C to 100 °C decreases the steady state fracture toughness by 29 %. The reason for this trend is likely to be related to the effects of temperature on the shear modulus of the resin and, consequently, on that of the composite ply. As shown in Table 2, the shear modulus of the ply shows a slight increase of 12 % (-50 °C). A more pronounced difference can be observed at 100 °C where the shear modulus decreases by 28 % when compared to the value measured at room temperature. Since the onset of fibre kinking depends on the shear modulus of the composite [36] any effect of temperature on the shear modulus will also affect the compressive failure of the longitudinal ply. For specimens tested in compression, that fail by kink-band formation, it can be observed (Table 3) that strength decreases with decreasing shear modulus.

Figure 20 shows that in the case of longitudinal tensile failure the maximum value of the intralaminar fracture toughness is obtained at room temperature. Increasing the temperature to 100 °C there is a decrease of 19 % on the steady-state value of the fracture toughness. A more drastic reduction of 70 % with respect to room temperature is obtained for -50 °C.

The calculated fracture process zone, using the size effect law, shows that in compression the value of  $l_{fpz}$  decreases with temperature. In compression,

$l_{fpz}$  corresponds to the region where a kink band is broadening. This trend  
 345 was observed for the range of temperatures under investigation. In tension, the  
 value of  $l_{fpz}$  decreases if there is a decrease or increase in the temperature when  
 compared to the same value at room temperature. This corresponds to a region  
 where the crack is still bridged by unbroken fibres. A more ductile response is  
 expected at 100 °C, however increasing the temperature modifies the residual  
 350 stress field at the fibre-matrix interface, due to the difference values of each  
 respective coefficient of temperature expansion, and thus modifying the process  
 of crack propagation.

The exact mechanisms that justify these observations need to be studied in  
 detail, possibly with the use of computational micromechanics. In any case, it  
 355 is apparent that the effect of temperature on the properties of the fibre-matrix  
 interface and on the local stress fields influence both the fracture toughness and  
 the length of the fracture process zone to a point where a quite brittle response  
 is obtained at -50 °C.

#### 4.4. SEM observations of the tensile specimens

360 Typical fracture surfaces at -50 °C and 100 °C are shown in Figures 21  
 and 22, respectively. There is a remarkable difference between the fracture  
 surfaces. The fracture surface at the lowest temperature is practically perpen-  
 dicular to the direction of the applied load with a very clean cleavage fracture  
 plane indicating a more brittle failure mode. At 100 °C, the fracture surface  
 365 presents irregular fragmented breaks in which some areas have bundles of fibres  
 without any supporting matrix. This is an indication of a more ductile fracture.

[Figure 21 about here.]

[Figure 22 about here.]

## 5. Conclusions

370 The method proposed to measure the fracture toughness of polymer com-  
 posites does not require any post processing or tracking of the crack position

during test. Therefore, the present method offers an advantage over alternative methods. The experiments can be performed without good visibility of the test specimen and crack tip position.

375 For the material used here, it was observed that some material properties are insensitive to the change in temperature (for the temperatures under investigation), such as the longitudinal Poisson's ratio. The longitudinal modulus was kept constant for all studied temperatures this is due to the challenges faced to measure this property under extreme temperature conditions.  $E_1$  is mainly  
380 controlled by the stiffness of the fibres and is unlikely to change in the range of temperatures considered in the present study.

The transverse and shear modulus decrease when the temperature increases.  $E_2$  decreases 14 % between -50 °C and room temperature and another 12 % when the temperature goes up to 100 °C. The shear modulus decreases 11 %  
385 from -50 °C to room temperature but the highest drop in value is observed when  $G_{12}$  is evaluated between RT and 100 °C where the value drops from 5.29 GPa to 3.83 GPa, which corresponds to a drop of 28 %. It is concluded that the temperature plays an important role in the fracture toughness of the composite material under investigation. By measuring the full R-curve, it is  
390 not only possible to assess the steady state value of the fracture toughness but also the length of the fracture process zone and their respective variations with temperature. Under compression, the steady state fracture toughness value does not change with the decreased in temperature to -50 °C but there is a decrease to 43.47 kJ/m<sup>2</sup> when the temperature is increased to 100 °C, which represents  
395 a 29 % decrease when compared to the  $\mathcal{R}_{SS}$  at room temperature. The fracture process zone decreases as the temperature decreases first by 24 % between 100 °C and room temperature, and then by 41 % between room temperature and -50 °C. In compression, where failure is by kink-band formation, the fracture process zone  $l_{fpz}$  corresponds to the region where the kink-band is broadening.

400 The maximum value of the tensile steady-state fracture toughness is obtained at room temperature ( $\mathcal{R}_{SS}^{RT}=205.31$  kJ/m<sup>2</sup>). The steady-state value of the tensile fracture toughness decreases when the temperature is increased to 100 °C

or decreased to  $-50\text{ }^{\circ}\text{C}$  taking the values of  $166.40\text{ kJ/m}^2$  and  $62.50\text{ kJ/m}^2$ , respectively. The fracture process zone follows the same trend where the highest value is measured at room temperature and equals  $2.63\text{ mm}$ . The length of the fracture process zone reduces rapidly when compared to the value obtained at  $100\text{ }^{\circ}\text{C}$  (73 % reduction). There is a drastic drop when looking at the result measured at  $-50\text{ }^{\circ}\text{C}$ , where the length of the fracture process zone is equal to zero. In tension,  $l_{fpz}$  corresponds to a region where there is bridging by unbroken fibres.

The SEM observations indicate that at cryogenic temperatures there is a brittle fracture where the fracture surface is perpendicular to the applied load direction and the surface itself has a constant topology. At high temperatures the fracture surface shows loose bundles of fibres without any supporting material. This is due to the softening of the matrix with the increase in temperature and subsequent decohesion events that take place in the interface between fibre and matrix.

Future work will attempt to further understand the observed trends by developing appropriate thermo-mechanical computational models developed at the micro-scale.

## 6. Acknowledgements

The present work was supported by the SHEFAE European project, FP7-AAT-2012-RTD-JAPAN, Grant agreement no. 314307.

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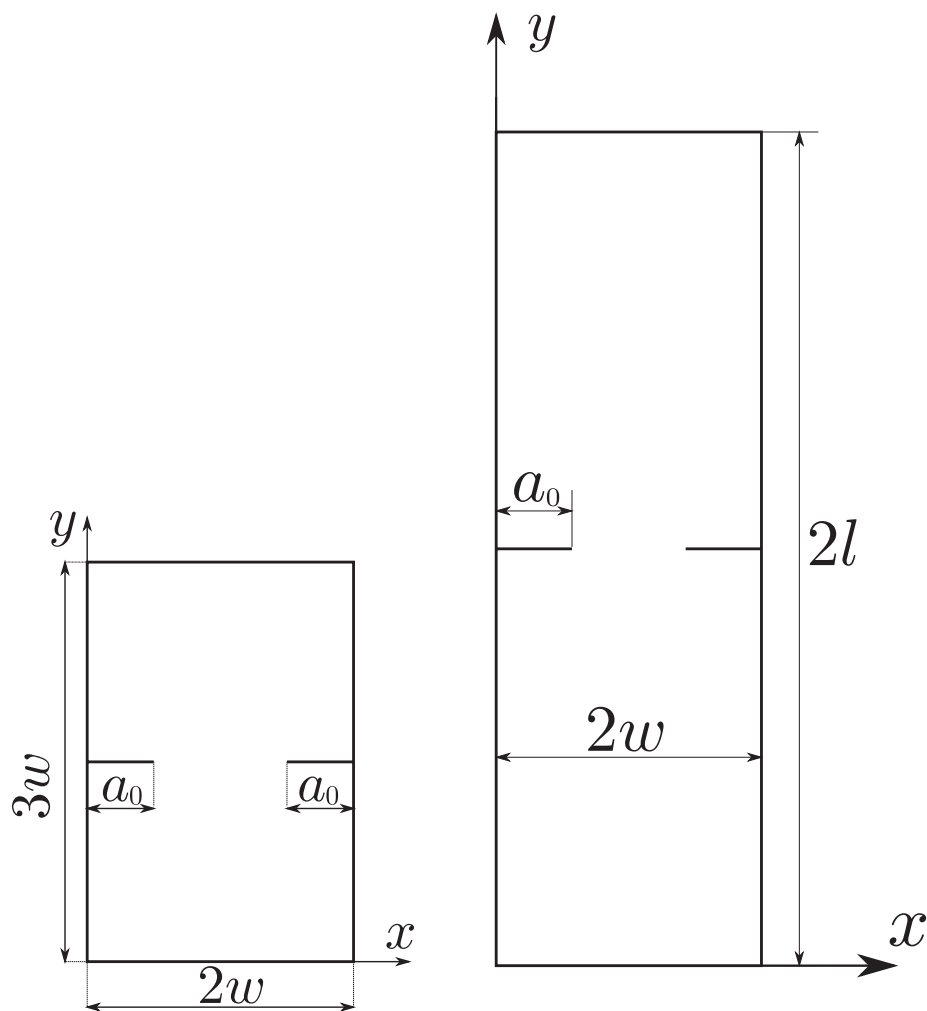


Figure 1: Double edge notched compression specimen (left) [19] and double edge notched tension specimen (right) [20].

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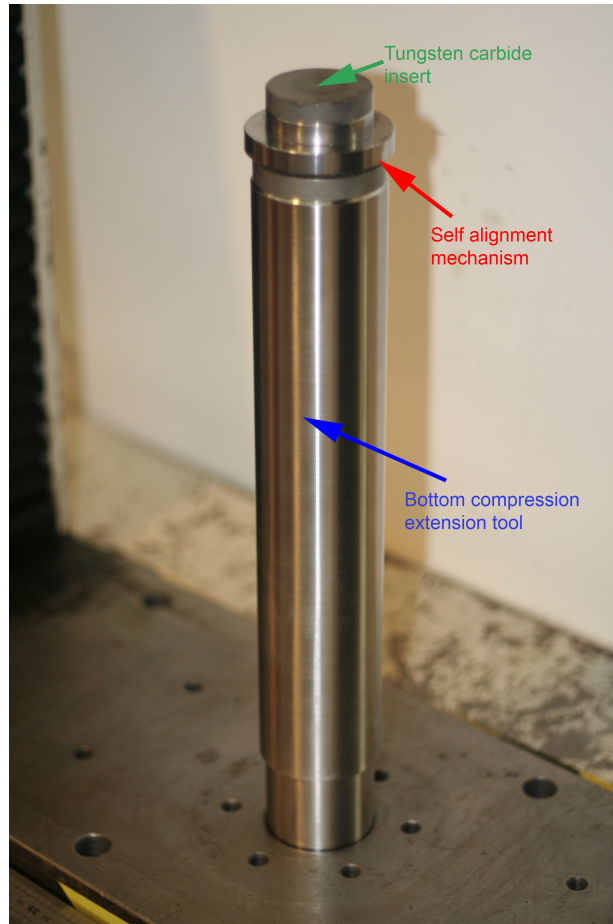


Figure 2: Bottom portion of the compressive testing rig showing the extension coupled with the self alignment mechanism.

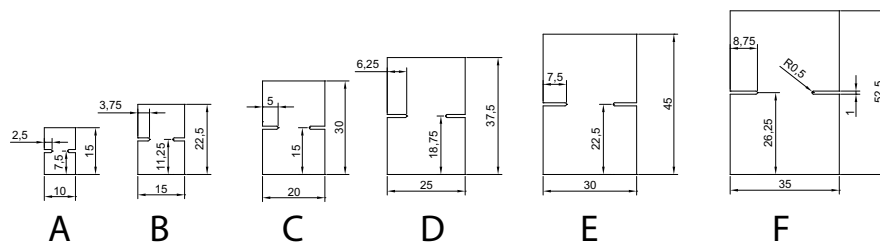


Figure 3: Compression specimen geometries showing dimensions from A to F in mm [19].

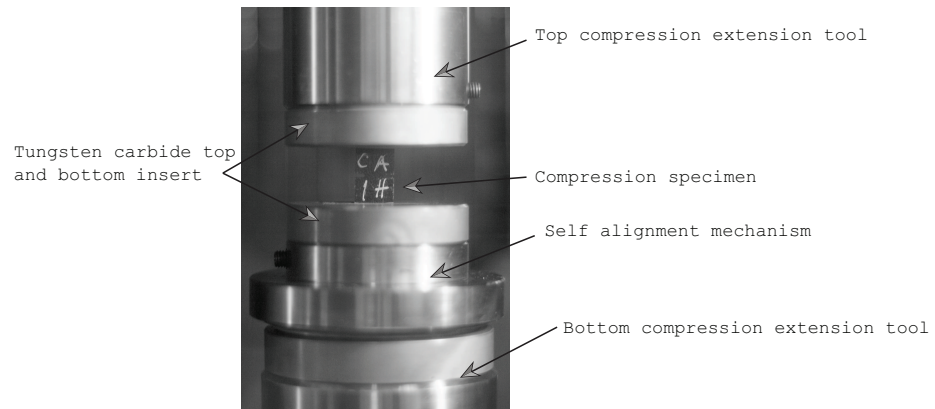


Figure 4: Compression specimen #1 from set A undergoing test at 100°C.

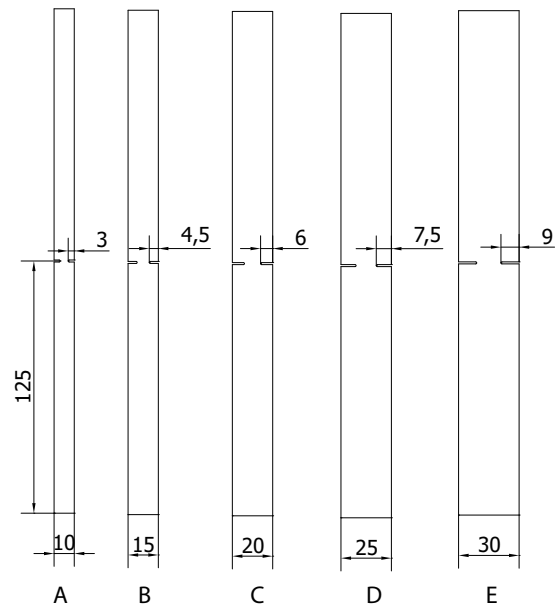


Figure 5: Tensile specimen geometries showing dimensions from A to E in mm.

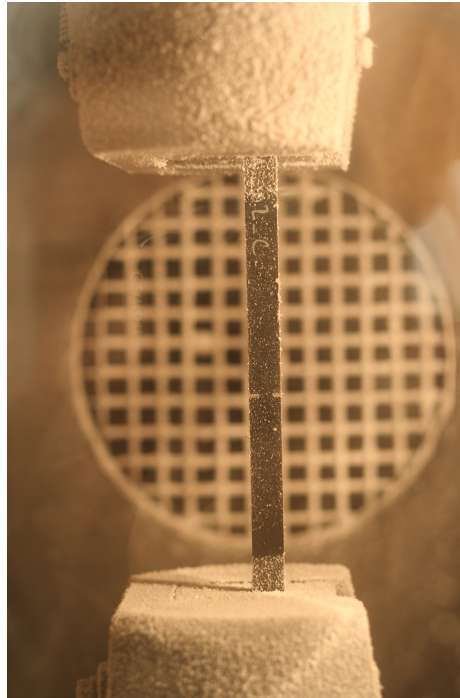
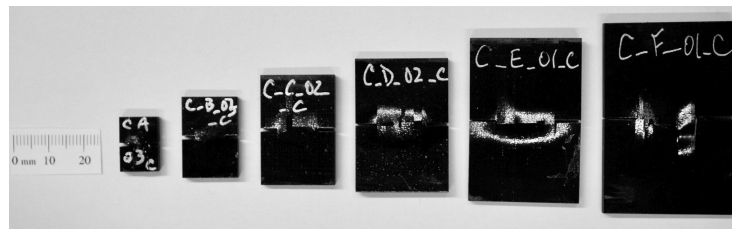
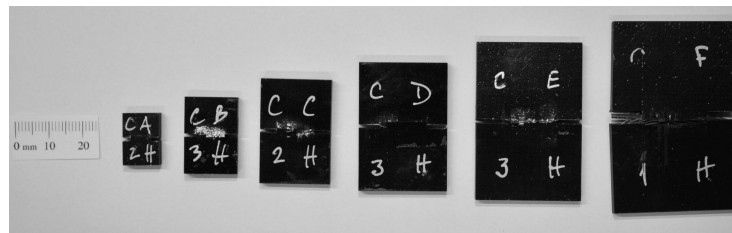


Figure 6: Geometry A tensile specimen #2 undergoing testing at  $-50^{\circ}\text{C}$ .



(a)



(b)

Figure 7: Compression specimens after testing at (a)  $-50^{\circ}\text{C}$  and (b)  $100^{\circ}\text{C}$ .



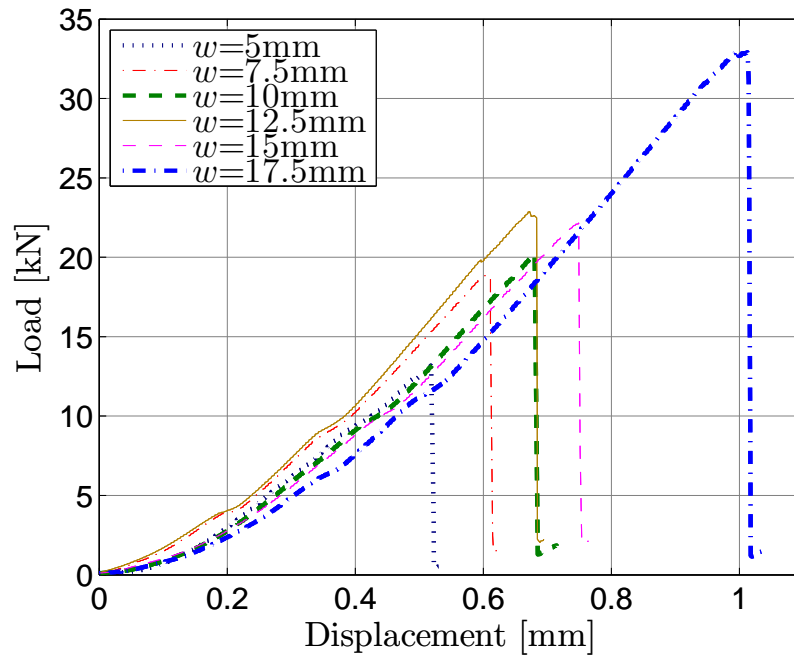


Figure 8: Load vs displacement curves for compression tests at  $-50^{\circ}\text{C}$ .

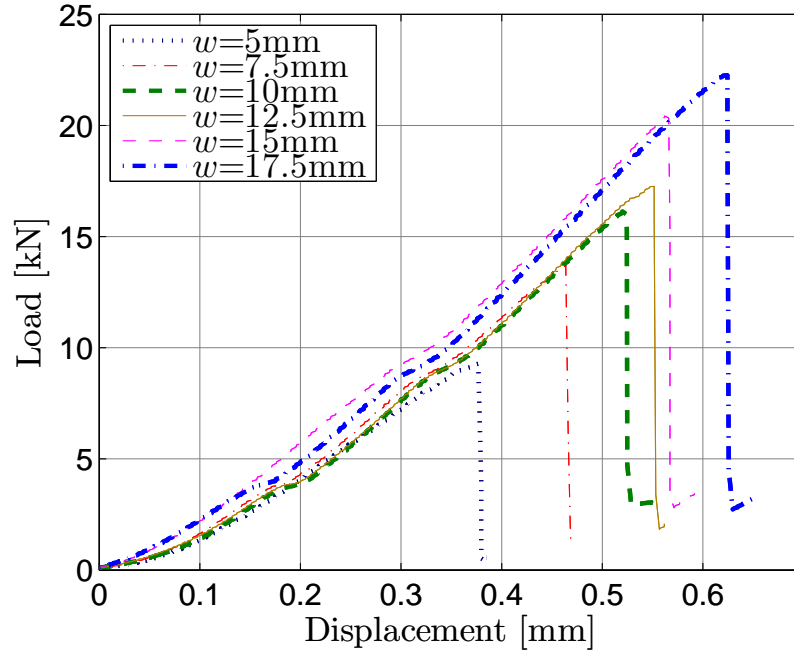
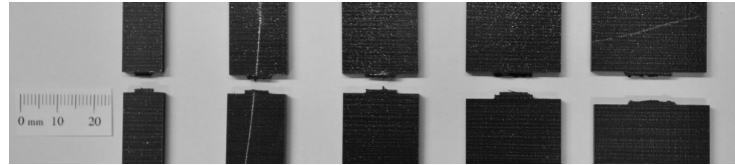
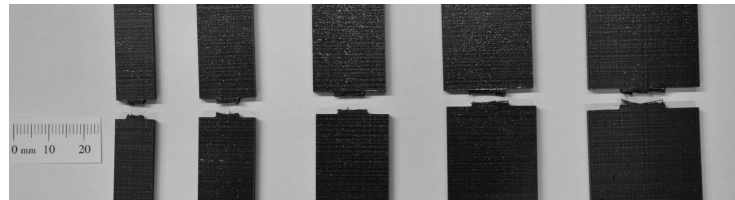


Figure 9: Load vs displacement curves for compression tests at 100°C.



(a)



(b)

Figure 10: Tension specimens after testing at (a)  $-50^{\circ}\text{C}$  and (b)  $100^{\circ}\text{C}$ .

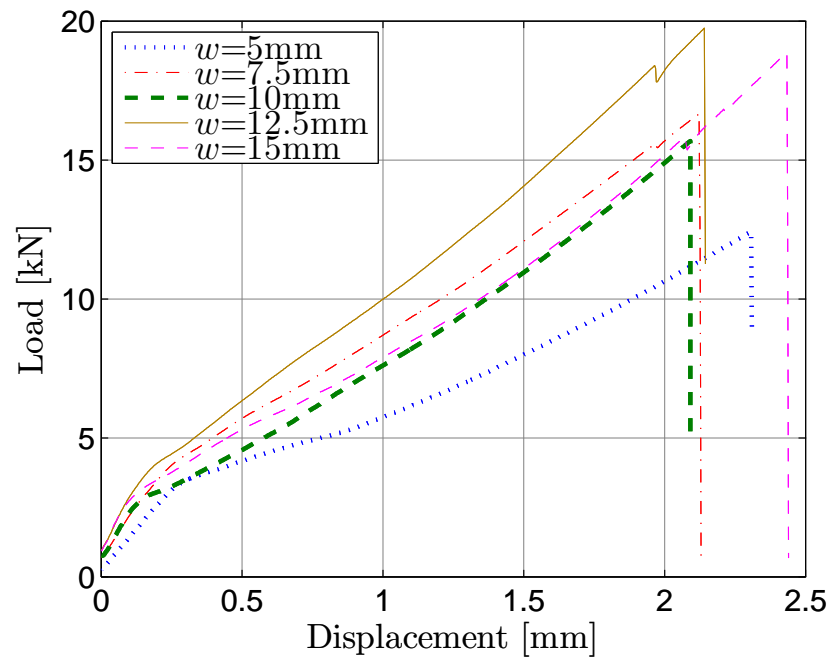


Figure 11: Load vs displacement curves for tension tests at  $-50^{\circ}\text{C}$ .

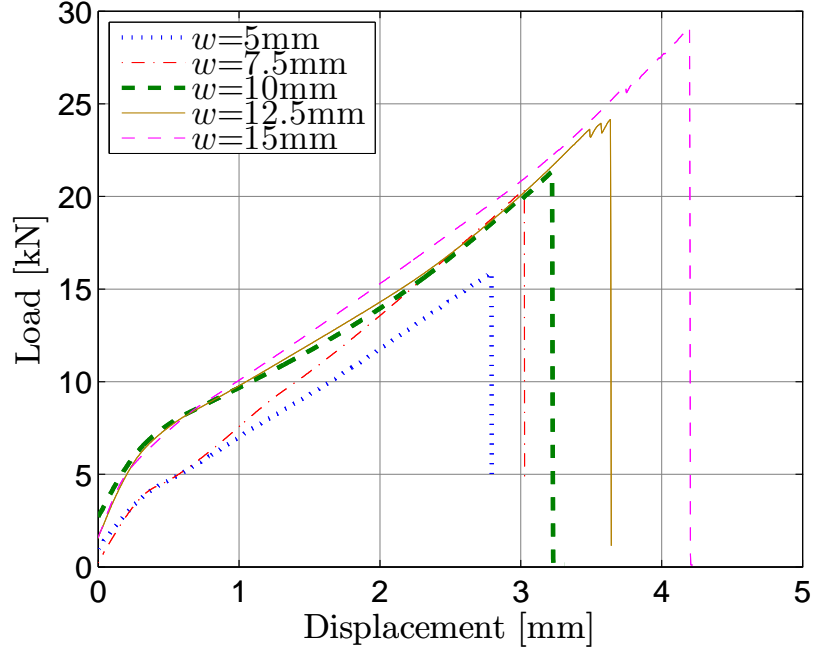


Figure 12: Load vs displacement curves for tension tests at 100°C.

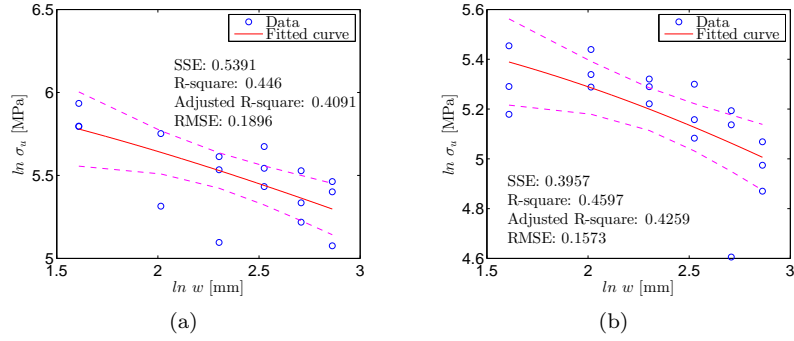


Figure 13: Size effect law and best fitting for compressive tests at (a)  $-50^{\circ}\text{C}$  and (b)  $100^{\circ}\text{C}$ .

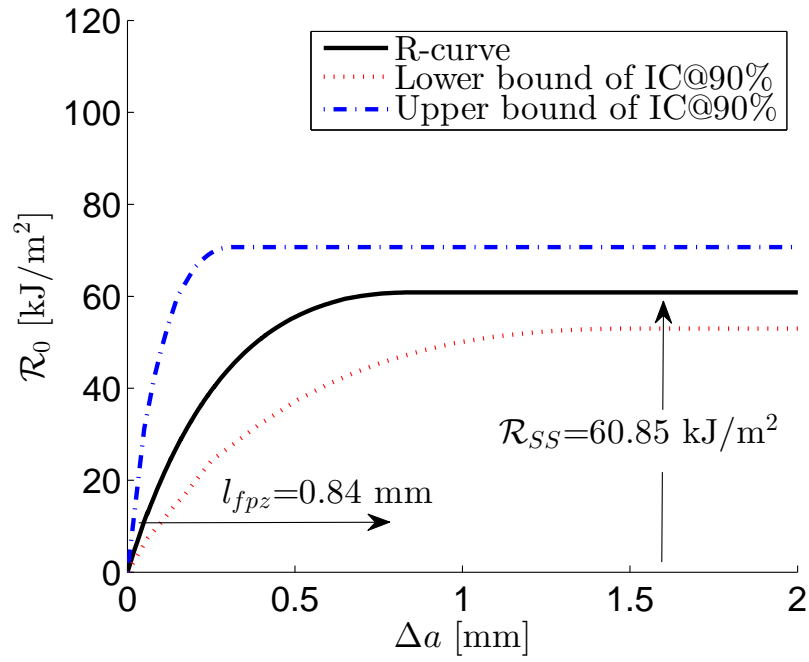


Figure 14: Envelope of the compressive crack driving force curves and R-curve for IM7/8552 at  $-50^\circ\text{C}$ .

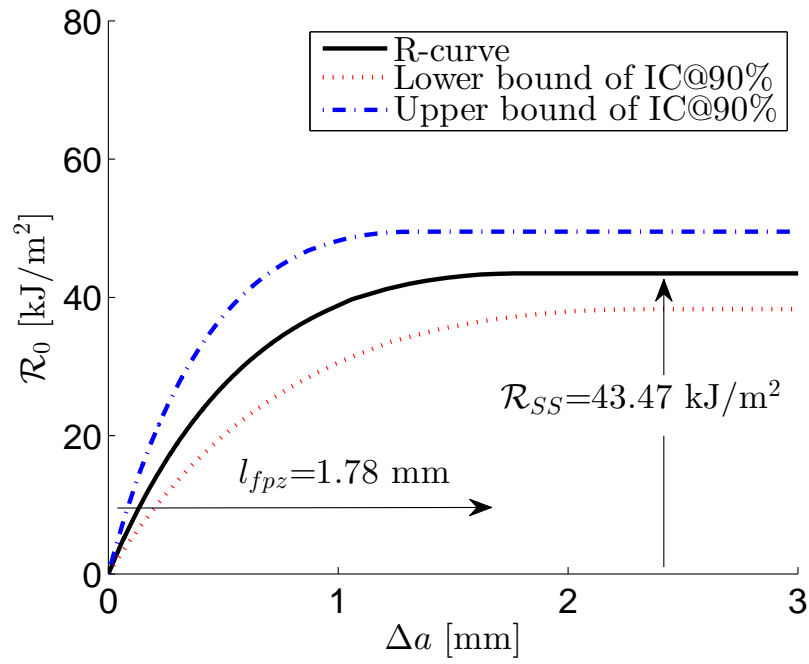


Figure 15: Envelope of the compressive crack driving force curves and R-curve for IM7/8552 at  $100^\circ\text{C}$ .

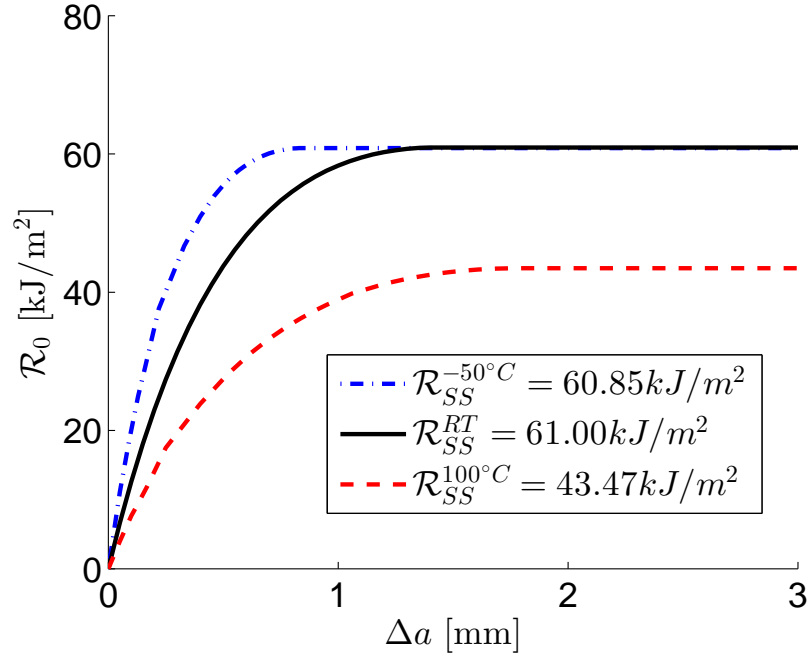


Figure 16: Compressive R-curve for IM7/8552 at  $-50^\circ\text{C}$ , room temperature [19] and  $100^\circ\text{C}$ .

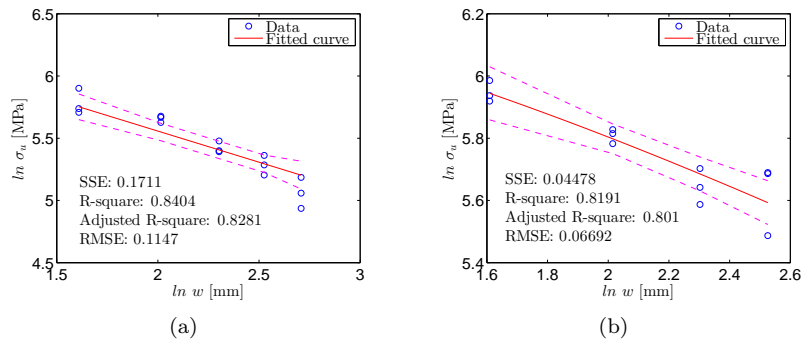


Figure 17: Size effect law and best fitting for tensile tests at (a)  $-50^\circ\text{C}$  and (b)  $100^\circ\text{C}$ .

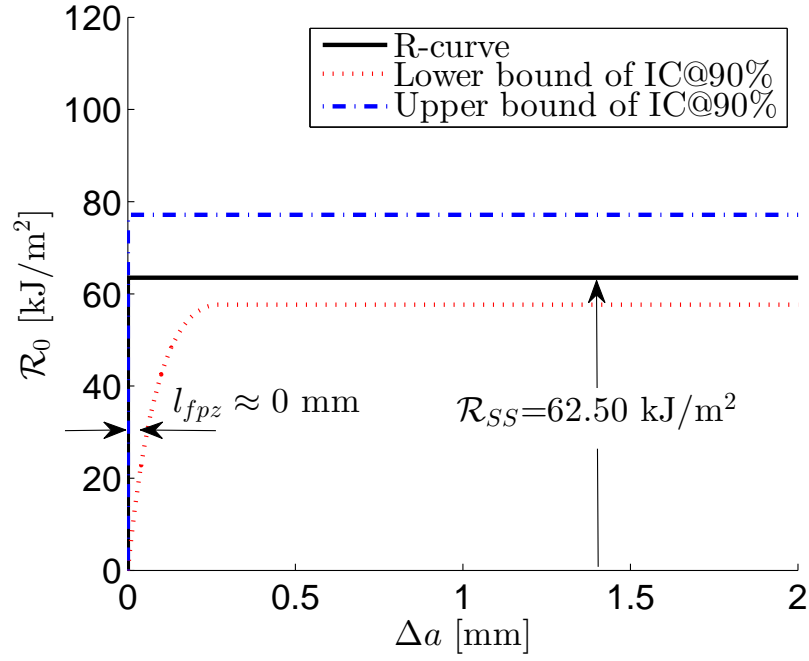


Figure 18: Envelope of the tensile crack driving force curves and R-curve for IM7/8552 at -50°C.

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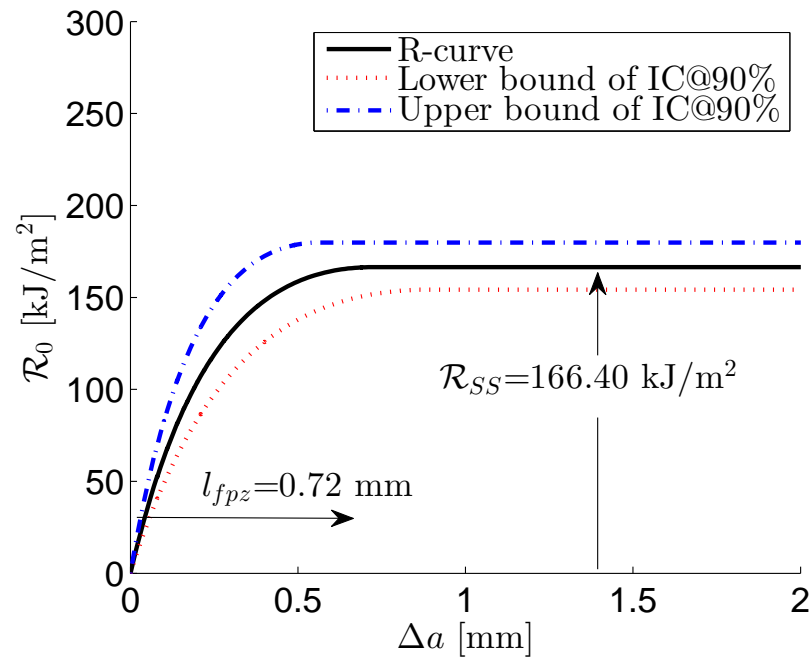


Figure 19: Envelope of the tensile crack driving force curves and R-curve for IM7/8552 at  $100^\circ\text{C}$ .

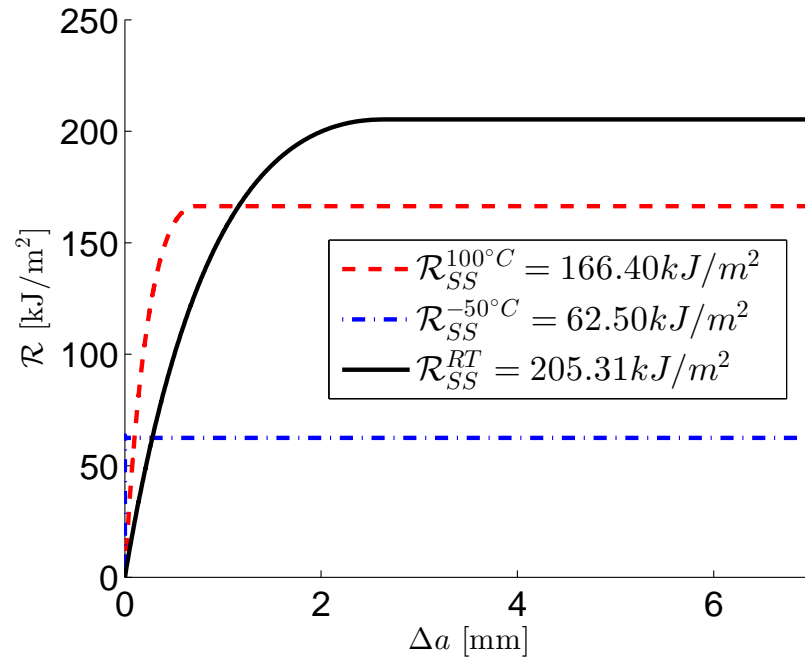


Figure 20: Tensile R-curve for IM7/8552 at  $-50^\circ\text{C}$ , room temperature [20] and  $100^\circ\text{C}$ .

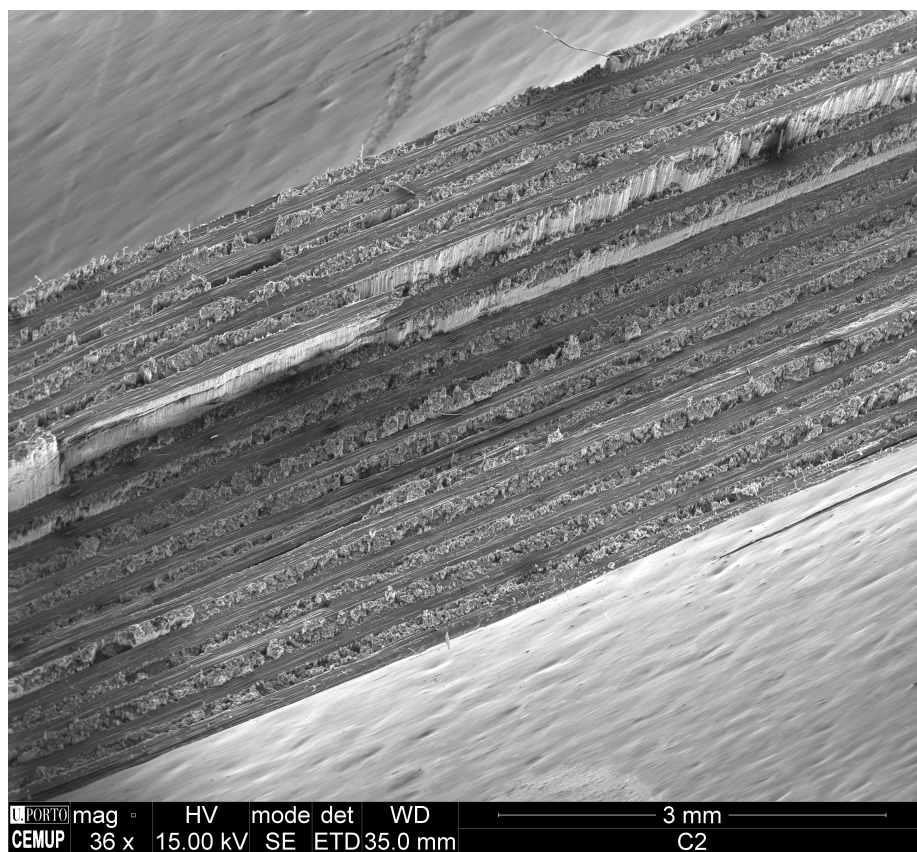


Figure 21: SEM fracture surface for DEN tensile specimen tested at  $-50^{\circ}\text{C}$ .

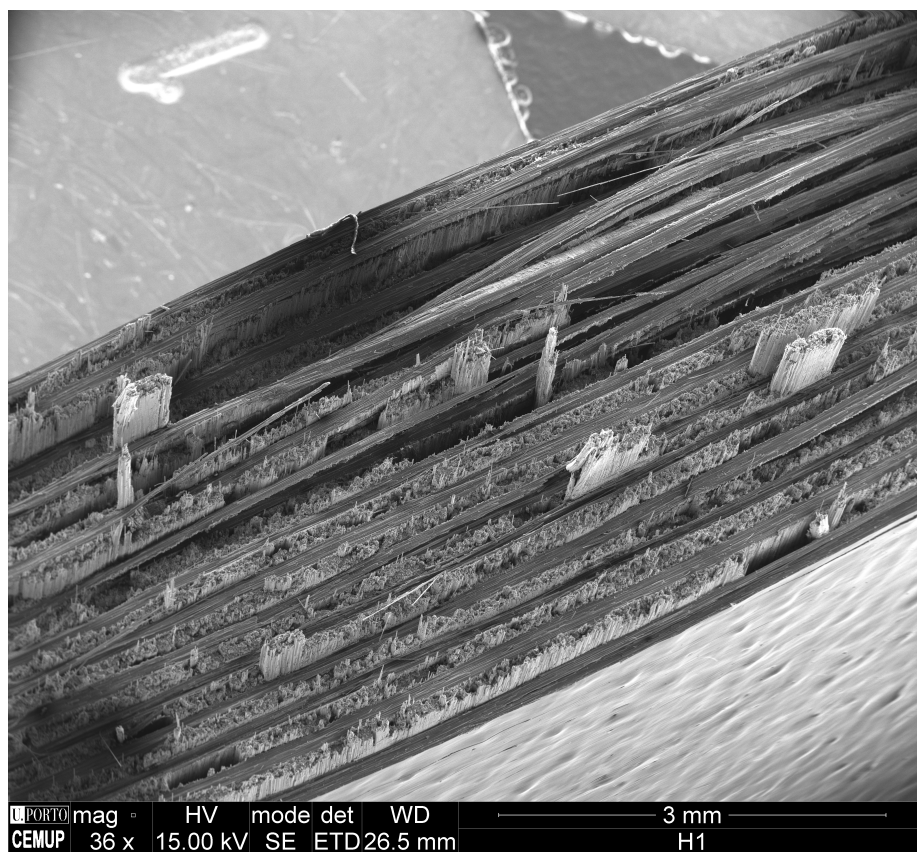


Figure 22: SEM fracture surface for DEN tensile specimen tested at 100°C.

Regression fit	Formula	Fitting parameters	$R_{SS}$	$l_{fpz}$
Bilogarithmic	$\ln \sigma_u = \ln \frac{M}{\sqrt{N+w}}$	$M, N$	$\frac{k_0^2}{E} M^2$	$\frac{k_0}{2k_0} N$
Linear regression I	$\frac{1}{\sigma_u^2} = Aw + C$	$A, C$	$\frac{k_0^2}{E} \frac{1}{A}$	$\frac{k_0}{2k_0} \frac{C}{A}$
Linear regression II	$\frac{1}{w\sigma_u^2} = \dot{A} \frac{1}{w} + \dot{C}$	$\dot{A}, \dot{C}$	$\frac{k_0^2}{E} \frac{1}{\dot{C}}$	$\frac{k_0}{2k_0} \frac{\dot{A}}{\dot{C}}$

Table 1: Size-effect laws and fitting parameters [27].

Temperature [°C]	$E_1$ [GPa]	$E_2$ [GPa]	$G_{12}$ [GPa]	$\nu_{12}$
-50	-	10.61	5.92	0.3287
RT [28]	171.42	9.08	5.29	0.32
100	-	7.96	3.83	0.3259
Standard	-	Ref. [29]	Ref. [30]	Ref. [29]

Table 2: IM7/8552 elastic properties at  $-50^\circ\text{C}$ , room temperature and  $100^\circ\text{C}$ .

Sample geometry	A	B	C	D	E	F
$2w$ [mm]	10	15	20	25	30	35
Area [mm <sup>2</sup> ]	40	60	80	100	120	140
$\bar{\sigma}_u^{-50^\circ\text{C}}$ [MPa]	345.17	259.10	230.18	258.48	214.62	205.90
STDV ( $\sigma_u^{-50^\circ\text{C}}$ ) [MPa]	23.01	55.77	47.98	25.58	27.88	32.86
$\bar{\sigma}_u^{100^\circ\text{C}}$ [MPa]	201.63	210.47	194.58	177.67	150.07	144.64
STDV ( $\sigma_u^{100^\circ\text{C}}$ ) [MPa]	23.28	13.40	8.05	15.86	35.61	11.69

Table 3: Summary of the compressive experimental results at  $-50^\circ\text{C}$  and  $100^\circ\text{C}$ .

Sample geometry	A	B	C	D	E
$2w$ [mm]	10	15	20	25	30
Area [mm <sup>2</sup> ]	40	60	80	100	120
$\bar{\sigma}_u^{-50^\circ C}$ [MPa]	325.80	286.40	226.72	197.56	158.38
STDV ( $\sigma_u^{-50^\circ C}$ ) [MPa]	28.33	6.18	8.96	12.70	16.07
$\bar{\sigma}_u^{100^\circ C}$ [MPa]	382.87	333.13	282.85	277.35	222.70
STDV ( $\sigma_u^{100^\circ C}$ ) [MPa]	10.76	6.28	13.34	25.34	14.62

Table 4: Summary of the tensile experimental results at  $-50^\circ\text{C}$  and  $100^\circ\text{C}$ .

Temperature [ $^\circ\text{C}$ ]	M [MPa $\sqrt{\text{mm}}$ ]	N [MPa $\sqrt{\text{mm}}$ ]	E [MPa]	$\alpha_0$	$\rho$
-50	898.30	2.71	91491	0.6	7.69
100	721.90	5.87	90056	0.6	11.73

Table 5: Summary of the required parameters to determine the R-curve in compression at  $-50^\circ\text{C}$  and  $100^\circ\text{C}$ .

Temperature [ $^\circ\text{C}$ ]	M [MPa $\sqrt{\text{mm}}$ ]	N [MPa $\sqrt{\text{mm}}$ ]	E [MPa]	$\alpha_0$	$\rho$
-50	704.40	$\approx 0$	91491	0.6	7.69
100	1035.00	2.36	90056	0.6	11.73

Table 6: Summary of the required parameters to determine the R-curve in tension at  $-50^\circ\text{C}$  and  $100^\circ\text{C}$ .